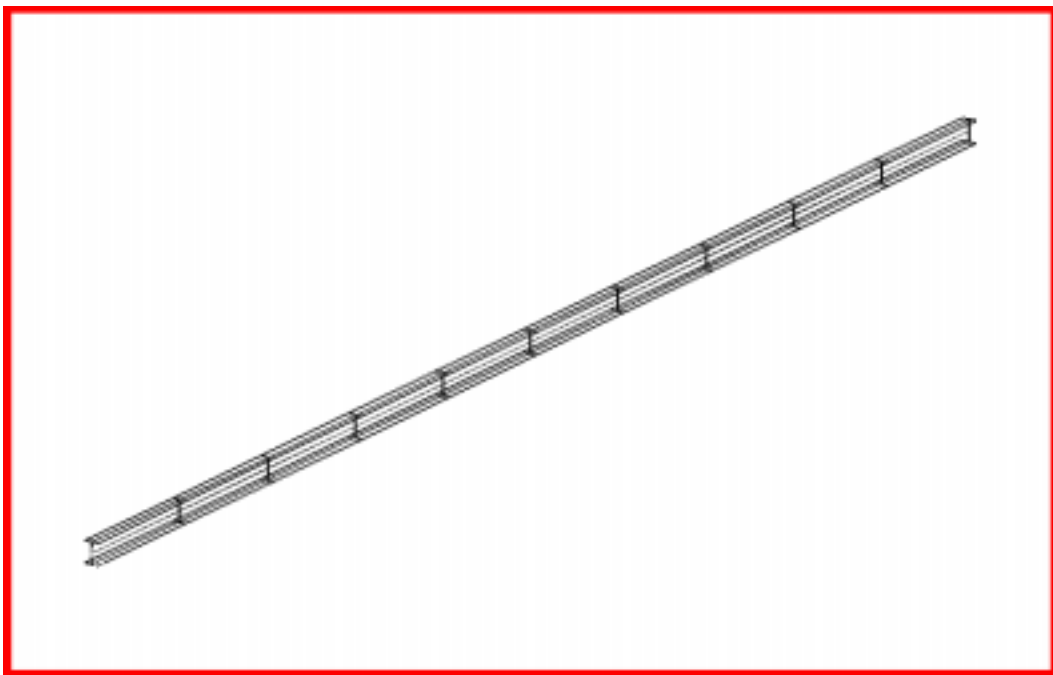


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**WORKSHOP PROBLEM 9b**

*Normal Modes with  
Differential Stiffness*



**Objectives**

- Analyze a stiffened beam for normal modes.
- Produce NASTRAN input file that represent beam and load.
- Submit for analysis.
- Find normal modes (natural frequencies).



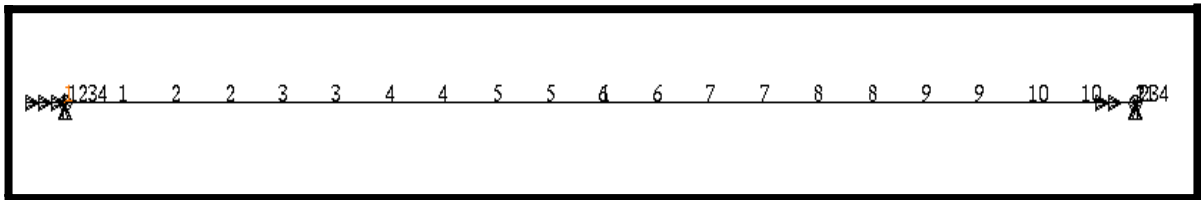
## Model Description:

The goal of this example is to analyze a stiffened model. In this case, the beam from Problem 9a. with a 500 lb force applied.

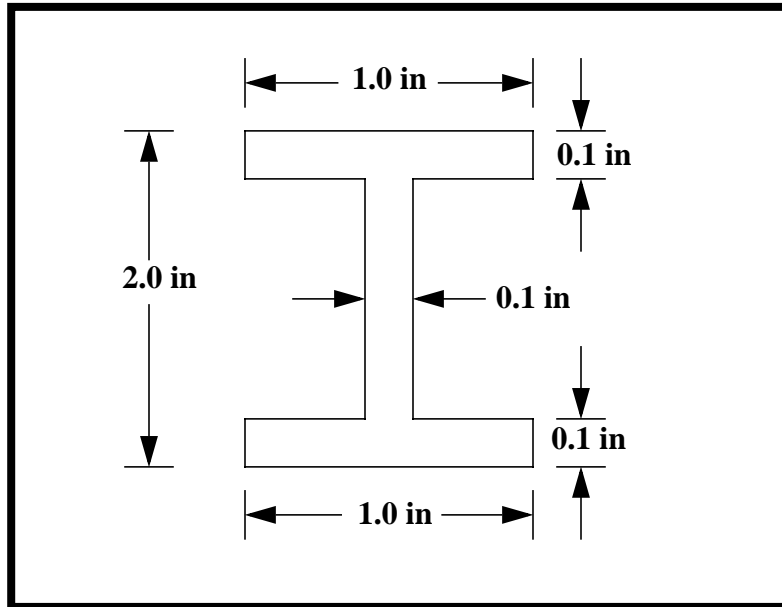
Figure 9b.1 below is a finite element representation of the beam. This is no longer a simple normal modes analysis. Instead we will be using a nonlinear static solution.

Below is a finite element representation of the beam. One end is pinned in 3 translations and one rotation. The other is pinned in 2 translations and one rotation with a 500 lb force applied.

**Figure 9b.1 - Grid Coordinates and Element Connectivities**



**Figure 9b.2 - Beam Cross Section**



**Table 9b.1 - Beam Dimensions**

<b>Length</b>	<b>100 in</b>
<b>Height</b>	<b>2 in</b>
<b>Width</b>	<b>1 in</b>
<b>Thickness</b>	<b>0.100 in</b>
<b>Area</b>	<b>0.38 in<sup>2</sup></b>
<b>I<sub>1</sub></b>	<b>0.229 in<sup>4</sup></b>
<b>I<sub>2</sub></b>	<b>0.017 in<sup>4</sup></b>

Theoretical Solution

$$f_n = \frac{K_n}{2\pi} \left[ \frac{EIg}{Wl^4} \left( 1 + \frac{1}{Kr} \frac{Pl^2}{EI} \right) \right]^{1/2}$$

For Mode 1,  $K_n=9.87$

$$f_n = \frac{9.87}{2\pi} \left[ \frac{10 \times 10^6 (0.229)(386.4)}{(0.38)(0.101)(100)^4} \times \left( 1 + \frac{1}{9.87} \frac{(500)(100)^2}{(10 \times 10^6)(0.229)} \right) \right]^{1/2}$$

$$f_n = 26.36 \text{ Hz}$$

For Static Load

$$\Delta = \frac{PL}{AE}$$

$$\Delta = \frac{500(100)}{0.38(10 \times 10^6)}$$

$$\Delta = 0.0132$$

---

## Exercise Procedure:

1. Start up MSC/NASTRAN for Windows 3.0 and begin to create a new model.

Double click on the icon labeled MSC/NASTRAN for Windows V3.0.

On the *Open Model File* form, select **New Model**.

*Open Model File:*

**New Model**

2. Import **prob1.DAT**.

**File/Import/Analysis Model...**

**Nastran**

**MSC/Nastran**

**OK**

Change the directory to **C : \temp**.

*File name:*

**prob9a.DAT**

**Open**

When asked, "Ok, to Adjust all massess by PARAM, WTMASS factor of 0.00259?", answer **No**. This information will be entered during analysis.

**No**

To reset the display of the model do the following.

**View/Redraw**

**View/Autoscale**

**OK**

3. Create the load set.

**Create/Load/Set...**

*Title:*

**pull**

**OK**

4. Define the options for a nonlinear analysis.

**Model/Load/Nonlinear Analysis...***Solution Type:*● **Static****Defaults...***Basic/Number of Increments:***5****OK**

5. Create the point loads.

**Model/Load/Nodal...**Select **Node 11**.**OK***(highlight)***Force***FX***500****OK****Cancel**

6. Submit the job for analysis.

**File/Export/Analysis Model...***Analysis Type:***10..Nonlinear Static****OK**Change the directory to **C:\temp**.*File name:***prob9b****Write****Run Analysis****Advanced...***Problem ID:***Normal Modes w/  
Differential Stiffness**

---

**OK**

Under *Output Requests*, unselect everything except:

**Displacement**

Also, change output to:

**2..Print and PostProcess**

**Type Input...**

*Current Line:*

**METHOD = 10**

**OK**

**OK**

Under *PARAM*, enter the following:

*WTMASS*

**.00259**

**Type Input...**

*Current Line:*

**PARAM, NMLOOP, 5**

**More**

*Current Line:*

**EIGRL, 10, , , 3**

**More**

*Current Line:*

**PARAM, COUPMASS, 1**

**OK**

**OK**

When asked if you wish to save the model, respond **Yes**.

**Yes**

*File name:*

**prob9b**

**Save**



When the MSC/NASTRAN manager is through running, MSC/NASTRAN will be restored on your screen, and the *Message Review* form will appear. To read the messages, you could select **Show Details**. Since the analysis ran smoothly, we will not bother with the details this time.

**Continue**

When asked if it is “OK to Begin Reading File C:\TEMP\prob9b.xdb”, respond **Yes**.

**Yes**

7. Determine the results of the analysis.

In order to find the 3 eigenvalues go to **C:/temp** and view the **prob9b.f06** file. Search for the section of the file that resembles the one shown on the next page.

Under *CYCLES*, what are the three natural frequencies?

1st = \_\_\_\_\_ Hz

2nd = \_\_\_\_\_ Hz

3rd = \_\_\_\_\_ Hz

Are the answers consistent with the theoretical solutions?

## R E A L E I G E N V A L U E S

MODE NO.	EXTRACTION ORDER	EIGENVALUE	RADIANS	CYCLES	GENERALIZED MASS	GENERALIZED STIFFNESS
1	1	##	##	##	##	##
2	2	##	##	##	##	##
3	3	##	##	##	##	##

8. List the displacement results of the analysis.

To list the displacement results, select the following:

**List/Output/Query...**

Under *the Output Set* pull down menu, what are the first three modes?

<i>Output Set:</i>	<input type="text" value="#..Case 1 Step 1.000000"/>
<i>Category:</i>	<input type="text" value="1..Displacement"/>
<i>Entity:</i>	<input type="radio"/> Node
<i>ID:</i>	<input type="text" value="11"/>
<input type="button" value="OK"/>	

What is the total displacement?

Displacement = \_\_\_\_\_

The answer is listed at the end of the exercise.

When finished, exit MSC/NASTRAN for Windows.

**File/Exit**

This concludes this exercise.

<i>Mode 1</i>	<b>26.360 Hz</b>
<i>Mode 2</i>	<b>98.033 Hz</b>
<i>Mode 3</i>	<b>217.434 Hz</b>
<i>Displacement</i>	<b>0.013158</b>

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